

Measuring and modeling diffuse scattering in protein X-ray crystallography

Andrew H. Van Benschoten^a, Lin Liu^a, Ana Gonzalez^b, Aaron S. Brewster^c, Nicholas K. Sauter^c, James S. Fraser^{a,1}, and Michael E. Wall^{d,1}

^aDepartment of Bioengineering and Therapeutic Sciences, University of California, San Francisco, CA 94158; ^bStanford Synchrotron Radiation Lightsource, SLAC National Accelerator Laboratory, Menlo Park, CA 94025; ^cMolecular Biophysics and Integrated Bioimaging Division, Lawrence Berkeley National Laboratory, Berkeley, CA 94720; and ^dComputer, Computational, and Statistical Sciences Division, Los Alamos National Laboratory, Los Alamos, NM 87545

Edited by Peter B. Moore, Yale University, New Haven, CT, and approved February 26, 2016 (received for review December 6, 2015)

X-ray diffraction has the potential to provide rich information about the structural dynamics of macromolecules. To realize this potential, both Bragg scattering, which is currently used to derive macromolecular structures, and diffuse scattering, which reports on correlations in charge density variations, must be measured. Until now, measurement of diffuse scattering from protein crystals has been scarce because of the extra effort of collecting diffuse data. Here, we present 3D measurements of diffuse intensity collected from crystals of the enzymes cyclophilin A and trypsin. The measurements were obtained from the same X-ray diffraction images as the Bragg data, using best practices for standard data collection. To model the underlying dynamics in a practical way that could be used during structure refinement, we tested translation–libration–screw (TLS), liquid-like motions (LLM), and coarse-grained normal-modes (NM) models of protein motions. The LLM model provides a global picture of motions and was refined against the diffuse data, whereas the TLS and NM models provide more detailed and distinct descriptions of atom displacements, and only used information from the Bragg data. Whereas different TLS groupings yielded similar Bragg intensities, they yielded different diffuse intensities, none of which agreed well with the data. In contrast, both the LLM and NM models agreed substantially with the diffuse data. These results demonstrate a realistic path to increase the number of diffuse datasets available to the wider biosciences community and indicate that dynamics-inspired NM structural models can simultaneously agree with both Bragg and diffuse scattering.

protein dynamics | normal modes | structural biology | diffuse scattering | liquid-like motions

X-ray crystallography can be a key tool for elucidating the structural basis of protein motions that play critical roles in enzymatic reactions, protein–protein interactions, and signaling cascades (1). X-ray diffraction yields an ensemble-averaged picture of the protein structure: each photon simultaneously probes multiple unit cells that can vary because of internal rearrangements or changes to the crystal lattice. Bragg analysis of X-ray diffraction only yields the mean charge density of the unit cell, however, which fundamentally limits the information that can be obtained about protein dynamics (2, 3).

An inherent limitation in Bragg analysis is that models with different concerted motions can yield the same mean charge density (4). The traditional approach assumes a single structural model with individual atomic displacement parameters (B factors). Given enough data, anisotropic displacement parameters can be modeled. When the data are more limited, translation–libration–screw (TLS) refinement, which models rigid-body motions of subdomains (5), is often used [22% of Protein Data Bank (PDB) depositions (6, 7)]. Variations in the TLS domains can predict very different motions that agree equally well with the Bragg data (8, 9).

Bragg analysis can be combined with additional information to model coupled motions in proteins. Patterns of steric clashes between alternative local conformations (10) can suggest certain modes of concerted motion, but the atomistic details may only be

reliably (yet indirectly) identified at high resolution. Time-averaged ensemble refinement (11) is another possibility, but it is complicated by the use of a TLS model to account for crystal packing variations (11). Solid-state NMR experiments (12) and long-time-scale molecular dynamics (MD) simulations (13–15) can be used to probe the structural basis of crystal packing variations and internal protein motions.

Extra information about protein motions can also be obtained in the X-ray crystallography experiment itself by analysis of diffuse scattering. Diffuse scattering arises when crystal imperfections cause X-rays to be diffracted away from Bragg reflections. When the deviations are due to crystal vibrations, they can be described using textbook temperature diffuse scattering theory (see, e.g., ref. 16). When each unit cell varies independently, the diffuse intensity is proportional to the variance in the unit cell structure factor (17), which describes correlations in the charge density variations. This assumption is appropriate when analyzing the broadly distributed diffuse intensity that corresponds to small correlation lengths (18–21), as the contribution of inter-unit cell atom pairs in this case is a small fraction of the total signal.

Several approaches have been used to connect macromolecular diffuse scattering data to models of protein motion and lattice disorder. Peter Moore (22) has emphasized the need to validate TLS models using diffuse scattering, as has been performed in a limited number of cases (8, 23, 24). Good agreement with the data

Significance

The structural details of protein motions are critical to understanding many biological processes, but they are often hidden to conventional biophysical techniques. Diffuse X-ray scattering can reveal details of the correlated movements between atoms; however, the data collection historically has required extra effort and dedicated experimental protocols. We have measured 3D diffuse intensities in X-ray diffraction from CypA and trypsin crystals using standard crystallographic data collection techniques. Analysis of the resulting data is consistent with the protein motions resembling diffusion in a liquid or vibrations of a soft solid. Our results show that using diffuse scattering to model protein motions can become a component of routine crystallographic analysis through the extension of commonplace methods.

Author contributions: A.H.V.B., N.K.S., J.S.F., and M.E.W. designed research; A.H.V.B., L.L., A.G., and M.E.W. performed research; A.H.V.B., L.L., A.S.B., N.K.S., and M.E.W. contributed new reagents/analytic tools; A.H.V.B., L.L., J.S.F., and M.E.W. analyzed data; and A.H.V.B., L.L., A.G., A.S.B., N.K.S., J.S.F., and M.E.W. wrote the paper.

The authors declare no conflict of interest.

This article is a PNAS Direct Submission.

Freely available online through the PNAS open access option.

Data deposition: The atomic coordinates and structure factors have been deposited in the Protein Data Bank, www.pdb.org (PDB ID codes 5F66 and 5F6M).

¹To whom correspondence may be addressed. Email: jfraser@fraserlab.com or mewall@lanl.gov.

This article contains supporting information online at www.pnas.org/lookup/suppl/doi:10.1073/pnas.1524048113/-DCSupplemental.

has previously been observed for liquid-like motions (LLM) models (18–21), which provide a softer model of the protein than the TLS model. In the LLM model, the atoms in the protein are assumed to move randomly, like in a homogeneous medium; the motions were termed “liquid-like” by Caspar et al. (19) because the correlations in the displacements were assumed to fall off exponentially with the distance between atoms.

Normal-modes (NM) models also treat the protein as a softer substance than the TLS model, but treat it as a solid. Normal-mode analysis (NMA) provides a more detailed picture of the conformational ensemble than the LLM model, enabling a direct connection to putative mechanisms of protein function (25). The NM refinement methods that have been developed for Bragg analysis use few additional parameters (26–30); however, these methods are not currently available in the standard builds of the major refinement software. Reasonable qualitative agreement previously has been seen using NM to model diffuse intensity in individual diffraction images (31, 32). More recently, the fit of alternative coarse-grained elastic network models to diffuse scattering data of staphylococcal nuclease has been investigated (33).

There is also a long-standing interest both in using diffuse scattering to validate improvements in MD simulations and in using MD to derive a structural basis for the protein motions that give rise to diffuse scattering (13, 31, 34–39). Recent advances in computing now enable microsecond duration simulations (13) that can overcome past barriers to accurate calculations seen using 10-ns or shorter MD trajectories (35, 38).

Despite the fact that diffuse scattering analysis is relatively well developed in small-molecule crystallography (40) and materials science (3), it has been underused in protein crystallography. There are relatively few examples of diffuse data analyzed using individual diffraction images from protein crystallography experiments, including studies of tropomyosin (41, 42), 6-phosphogluconate dehydrogenase (43), yeast initiator tRNA (44), insulin (19), lysozyme (20, 23, 24, 31, 32), myoglobin (38), Gag protein (45), and the 70s ribosome subunit (46). Moreover, there are an even smaller number of examples involving complete 3D diffuse datasets; these include studies of staphylococcal nuclease (21) and calmodulin (18).

To exploit diffuse scattering for modeling protein motions, there is a pressing need to increase the number of proteins for which complete 3D diffuse datasets have been experimentally measured. Conventional data collection procedures use oscillation exposures to estimate the full Bragg intensities. In contrast, the complete 3D datasets measured by Wall et al. (18, 21) used specialized methods for integrating 3D diffuse data from still diffraction images. Similar methods now can be generalized and applied to other systems using modern beamlines and X-ray detectors. In particular, the recent commercial development of pixel-array detectors (PADs), which possess tight point-spread functions and single-photon sensitivity (47), have created opportunities for measuring diffuse scattering as a routine tool in protein crystallography experiments using more conventional data collection protocols.

Here, we present diffuse scattering datasets for the human proline isomerase cyclophilin A (CypA) and the bovine serine protease trypsin. These datasets substantially increase the amount of experimental 3D diffuse scattering data available to the macromolecular crystallography community, providing a necessary foundation for further advancement of the field (48). To assess the potential for routine collection of diffuse datasets in crystallography, rather than expending a great deal of effort in optimizing the diffuse data and collecting still images (18, 21), we used oscillation images obtained using best practices for high-quality Bragg data collection. The resulting datasets yield 3D diffuse data that can discriminate among alternative TLS refinements (8), LLM models (19, 20), and NM models (32–34). Moreover, the agreement of the NM models with both Bragg and diffuse scattering data suggests a path forward for using both data sources simultaneously with a small number of variables. Our results demonstrate that diffuse intensity can, and

should, be measured in a typical X-ray crystallography experiment and indicate that diffuse scattering can be applied broadly as a tool to understand protein motions.

Results

Experimental Diffuse Data Show Crystallographic Symmetry. We obtained nearly complete 3D anisotropic diffuse datasets D' for CypA and trypsin using a PAD detector with synchrotron radiation (Methods, Fig. 1, and SI Appendix, Fig. S1), and used the Friedel and Laue group symmetry to quantify the level of crystallographic symmetry. We averaged intensities between Friedel pairs to create a symmetrized map D'_F and calculated the linear correlation CC_F between D' and D'_F . For CypA and trypsin, $CC_F = 0.90$ and 0.95 , respectively. We averaged P222-related reflections (corresponding to the $P2_12_12_1$ space group of both CypA and trypsin) to produce the Laue symmetrized intensities, D'_L . The linear correlation CC_L was then computed between D' and D'_F , yielding $CC_L = 0.70$ for CypA and $CC_L = 0.69$ for trypsin. These correlations indicate the experimental diffuse intensity follows the Bragg peak symmetry.

TLS Models Yield Low Correlation with Diffuse Scattering Data. To investigate how well TLS models agree with the molecular motions in the CypA crystal, we compared the experimental diffuse data to intensities calculated from three alternative TLS models: “Phenix,” “TLSMD,” and “whole-molecule” (SI Appendix, Fig. S2 A–D). Although all three models predict different motions, the R factors are very similar: R,R-free = 16.4%, 18.1% for the whole-molecule and Phenix models; and 16.2%, 18.1% for the TLSMD model. The correlations between the calculated diffuse intensity for these models and the anisotropic experimental data are low: 0.03 for the phenix model; 0.04 for the TLSMD model; and 0.14 for the whole-molecule model. In addition, the pairwise correlations of the calculated diffuse intensities are low: 0.066 for whole-molecule/TLSMD; 0.116 for whole-molecule/Phenix; and 0.220 for Phenix/TLSMD.

Like CypA, the three trypsin TLS models (SI Appendix, Fig. S2 E–H) yielded very similar R,R-free values: 15.1%, 16.7% for the whole-molecule model; 15.3%, 16.6% for the Phenix model; and

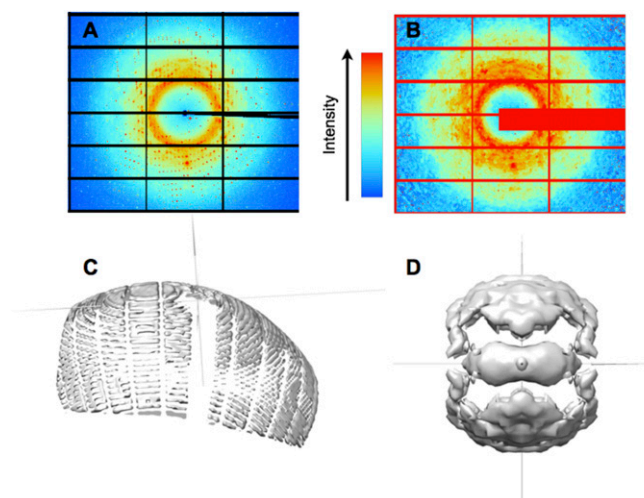


Fig. 1. Steps in diffuse data integration. (A) Raw CypA diffraction images are processed (B) to remove Bragg peaks and enable direct comparisons of pixel values to models. (C) Pixels in diffraction images are mapped to reciprocal space and values of diffuse intensity are accumulated on a 3D lattice; each diffraction image produces measurements of diffuse intensity on the surface of an Ewald sphere. (D) The data from individual images are combined and symmetrized to yield a nearly complete dataset (isosurface at a value of 65 photon counts in the total intensity, before subtracting the isotropic component).

15.2%, 16.6% for the TLSMD model. Correlations between the calculated and experimental diffuse intensities are again low: 0.02 for the Phenix and TLSMD models, and 0.08 for the whole-molecule model. Comparisons of the calculated anisotropic diffuse intensity show that the whole-molecule motion is dissimilar to both the Phenix and TLSMD predictions ($CC = 0.03$ and 0.05 , respectively). In contrast, the Phenix and TLSMD models yield much more similar diffuse intensities ($CC = 0.515$). The relatively high correlation between these models is consistent with the similarity in the TLS groups (*SI Appendix, Fig. S2 F–H*). The low correlation of the CypA and trypsin TLS models with the diffuse data suggests that the protein motions might be correlated on a shorter length scale than provided by these models.

LLM Models Yield Substantial Correlation with Diffuse Scattering Data. One model that accounts for short-range correlations is LLM (19, 20). The LLM model assumes that atomic displacements are uncorrelated between different unit cells, but are correlated within the unit cells. The correlation in the displacements is assumed to decay exponentially as $e^{-x/\gamma}$, where x is the separation of the atoms, and γ is the length scale of the correlation. The displacements of all atoms are assigned a SD of σ . The LLM model previously has been refined against 3D diffuse intensities obtained from crystalline staphylococcal nuclease (21) and calmodulin (18), yielding insights into correlated motions.

We refined isotropic LLM models of motions in CypA and trypsin against the experimental diffuse intensities (*Methods*). The CypA model was refined using data in the resolution range of 31.2–1.45 Å, and the trypsin model using 68–1.46-Å data. For CypA, the refinement yielded $\gamma = 7.1$ Å and $\sigma = 0.38$ Å with a correlation of 0.518 between the calculated and experimental anisotropic intensities. The highest correlation between data and experiment occurs in the range of 3.67–3.28 Å, where the value is 0.74 (Fig. 2A). For the trypsin dataset, the refinement yielded $\gamma = 8.35$ Å and $\sigma = 0.32$ Å with a correlation of 0.44, which is lower than for CypA. The peak value is 0.72 in the resolution range of 4.53–4.00 Å (Fig. 2B).

The refined LLM models also were compared with the data using simulated diffraction images. Images corresponding to frame number 67 of the CypA data were obtained using the LLM model (Fig. 3A) and the 3D diffuse data (Fig. 3B). The main bright features above and below the origin are similar between the two.

Many of the weaker features also appear to be similar, both at high and low resolution. The similarity is diminished but still apparent for images obtained for frame number 45 of trypsin (*SI Appendix, Fig. S3*). These simulations provide a visual confirmation of the substantial correlations obtained for the 3D diffuse intensity (see *SI Appendix, Fig. S1*, for visualization comparisons of the LLM model to the diffuse data in 3D).

Normal Modes Can Model Both Diffuse and Bragg Scattering Data. To assess the potential of NMA to be developed for diffuse scattering studies, we developed coarse-grained elastic network models of the CypA and trypsin unit cells. The C_{α} coordinates and B factors for the NM models of diffuse scattering are by definition identical to those derived from the Bragg data (*Methods*). To assess the agreement of specific NM-derived conformational variations with the Bragg data, we eliminated the B factor constraint and generated 50-member ensembles from the 10 lowest-frequency nonzero modes (*Methods*). To more accurately model the Bragg data, we adjusted the overall spring constant and applied an additional uniform isotropic B factor to all atoms (*Methods* and *SI Appendix, Fig. S4*). The correlations were high across resolution shells (Fig. 2C and D), yielding overall R factors of 38% (CypA) and 31% (trypsin) (*SI Appendix, Tables S1 and S2*). We also calculated the predicted diffuse intensity from the NM models: the correlation of the CypA model with the data is 0.41 in the resolution range of 31.2–1.45 Å, and the correlation of the trypsin model with the data is 0.38 in the resolution range of 68–1.46 Å. The agreement with the data is substantial within individual resolution shells (Fig. 2). The NM simulated diffraction image for CypA (Fig. 3C) shows bright features that are found in the data (Fig. 3B). The relative strength at high versus low resolution is greater than in the data, however, suggesting that this NM model is too rigid; this discrepancy might be addressed by softening the intraresidue interactions and optimizing the model against the diffuse scattering data directly. The comparisons of simulated diffraction images for trypsin are consistent with the findings for CypA (*SI Appendix, Fig. S3*).

Discussion

Diffuse X-ray scattering is a potentially valuable yet little exploited source of information about macromolecular dynamics. Diffuse intensities can double the total number of measured data points in

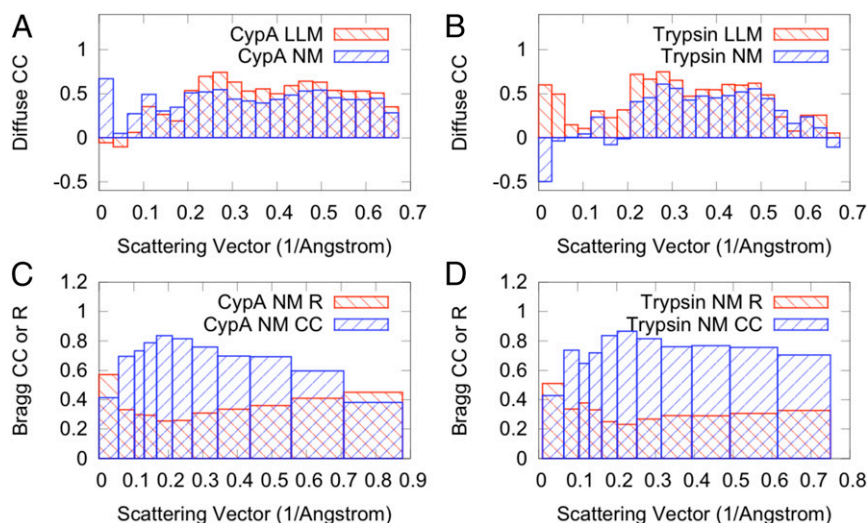


Fig. 2. Agreement of models of protein motions with diffuse and Bragg data. (A and B) Linear correlation coefficients (CCs) between diffuse data and LLM (red bars) or NM models (blue bars) computed by resolution shell for (A) CypA and (B) trypsin. (C and D) Correlations and R factors between Bragg data and NM models computed by resolution shell for (C) CypA and (D) trypsin. Agreement factors for the diffuse and Bragg data were computed using LUNUS (60) and Phenix (67), respectively.

measurements of ribosome crystals, which indicates that models should simultaneously account for correlations that are coupled both within and across unit cell boundaries (18, 20); accounting for lattice vibrations more accurately also might yield improved Bragg integration (48). Moreover, comparisons of crystal simulations and diffuse scattering can provide an additional observable for benchmarking improvements in energy functions and sampling schemes (14).

Although the initial successes of dynamics-based models of diffuse scattering indicate that crystal defects can play a secondary role in contributing to the diffuse signal, at least in some cases, consideration of crystal defects might become important to achieve the highest model accuracy and most general applicability of diffuse scattering in crystallography. Additionally, as more X-ray data from both brighter conventional and X-ray free-electron laser light sources, accounting for all sources of Bragg and diffuse scattering will be necessary to model the total scattering needed for innovative phasing applications (59). In summary, the datasets presented here demonstrate that diffuse scattering can now be routinely collected and that using these data will help us obtain an increasingly realistic picture of motion in protein crystals, including integrated descriptions of intramolecular motions, lattice vibrations, and crystal defects.

Methods

Diffuse Data Integration. After conventional crystallization, data collection, and processing (*SI Appendix, Supplementary Text: Methods*), image processing was performed, using the LUNUS collection of diffuse scattering tools (60), to transform raw images (Fig. 1A) into ones in which the pixel values could be used to integrate 3D datasets (Fig. 1B). The beam stop and image edges were masked, as were pixel values outside of the range 1–10,000 photon counts. A beam polarization correction and solid-angle normalization were applied (60). Bragg peaks were removed using mode filtering with a mask width of 20 pixels and a histogram bin of one photon count.

Diffuse data integration was performed using a python script that calls DIALS methods within the Computational Crystallography Toolbox (CCTBX) (61, 62). The script obtains an indexing solution and uses the results to map each pixel in each diffraction image to fractional Miller indices $h'k'l'$ in reciprocal space. It sums the intensities from pixels in the neighborhood of each integer Miller index hkl and tracks the corresponding pixel counts, while ignoring pixels that fall within a $1/2 \times 1/2 \times 1/2$ region about hkl . It writes the intensity sums and pixel counts for each frame on a grid, populated on an Ewald sphere that varies according to the crystal orientation for each image (Fig. 1C). Lunus methods were used to obtain a radial scattering vector intensity profile for each frame, which was used for scaling. The mean diffuse intensity was calculated at each grid point using the scaled sums and pixel counts from all of the frames. The integration yielded a CypA dataset with 438,627 measurements that is 98% complete to a resolution of 1.4 Å, and a trypsin dataset with 233,381 measurements that is 95% complete to 1.25-Å resolution.

Experimental and model diffuse intensities were compared using just the anisotropic component of the signal, which is primarily due to the protein (13). Lunus methods were used to subtract the radial average and obtain the anisotropic signal. Intensities were symmetrized by averaging P222-equivalent points. The comparable degree of symmetry in the CypA and trypsin data suggests that the measurement of diffuse intensity is robust with respect to the difference in the phi angle oscillation during data collection (0.5° for CypA vs. 1° for trypsin).

All images are available on SBGrid Data Grid (<https://data.sbgrid.org/dataset/68/> for CypA; <https://data.sbgrid.org/dataset/201/> for trypsin), and the symmetrized datasets are available in [Datasets S1](#) and [S2](#).

Simulated Diffraction Images. Diffuse scattering images were simulated using methods similar to those for data integration. A template frame was used to map each pixel to a fractional Miller index. The new value of each pixel was obtained by linear interpolation between the nearest-neighbor integer points hkl in the 3D diffuse model or data. In the case of the 3D data, the images greatly enhanced the diffuse features compared with the raw images (*SI Appendix, Figs. S5 and S6*) because of statistical averaging in data integration. For visualization of simulated images, the minimum pixel value was computed within each pixel-width annulus about the beam center, and was subtracted from each pixel value within the annulus. Images were displayed using Adxv version 1.9.10 (63), with display parameters selected for meaningful comparison of the diffuse features.

TLS Structure Refinement and Diffuse Scattering Model. Three independent TLS refinements were performed for CypA (*SI Appendix, Fig. S2 A–D*). The whole-molecule selection consists of the entire molecule as a single TLS group. The Phenix selection consists of the eight groups (residues 2–14, 15–41, 42–64, 65–84, 85–122, 123–135, 136–145, and 146–165) identified by phenix.find_tls_groups. The TLSMD selection consists of eight groups (residues 2–15, 16–55, 56–80, 81–85, 86–91, 92–124, 125–143, and 144–165) identified by the TLS Motion Determination web server (6, 7). All TLS refinement was performed within phenix.refine through five macrocycles. Aside from the inclusion of TLS refinement, these macrocycles were identical to the initial structure refinement described above.

Similarly, for trypsin, we selected whole-molecule, Phenix, and TLSMD TLS refinement strategies as described above (*SI Appendix, Fig. S2 E–H*). The Phenix selection consists of seven TLS groups: residues 16–54, 55–103, 104–123, 124–140, 141–155, 156–225, and 226–245. The TLSMD selection consists of nine groups: residues 16–52, 53–98, 99–115, 116–144, 145–171, 172–220, 221–224, 225–237, and 238–245.

Structural ensembles were generated using the phenix.tls_as_xyz method (9). One thousand random samples were drawn assuming independent distributions for each domain. Diffuse intensities were calculated using phenix.diffuse (8). CypA and trypsin models were generated to a final resolution of 1.2 and 1.4 Å, respectively.

LLM Model. LLM models of diffuse scattering were calculated using PDB entries 5F66 (CypA) and 5F6M (trypsin). Temperature factors were set to zero and squared calculated structure factors $I_0(hkl)$ were computed using the `structure_factors`, `as_intensity_array`, and `expand_to_p1` methods in CCTBX (61, 62). The Lunus `symtl` method was used to complete the grid using the P222 Laue group.

Given a correlation length γ and amplitude of motion σ , the diffuse intensity at scattering vector \mathbf{s} was calculated as $D_{LLM}(\mathbf{s}) = 4\pi s^2 \sigma^2 e^{-4\pi^2 s^2 \sigma^2} I_0(\mathbf{s})^* \Gamma_\gamma(\mathbf{s})$, with $\Gamma_\gamma(\mathbf{s}) = 8\pi\gamma^3/(1 + 4\pi^2 s^2 \gamma^2)$. Fourier methods in Lunus (ffttf) were used for the convolution. The linear correlation of the anisotropic intensities with the data was used as a target function for refinement. Optimization of the target with respect to γ and σ was performed using the Powell minimization method.

NM Model. The NM model followed methods similar to those of Riccardi et al. (33). Atomic coordinates and isotropic displacement parameters were obtained from PDB entries 5F66 (CypA) and 5F6M (trypsin), and were expanded to the P1 unit cell using the *iotbx.pdb* methods in CCTBX (62). The Hessian matrix \mathbf{H} was defined using a modified anisotropic elastic network model (64), with springs between C_α atoms (i, j) within a cutoff radius of 25 Å. The spring force constants were computed as $k e^{-r_{ij}/\lambda}$, where r_{ij} is the closest distance between atoms i and j , either in the same unit cell or in neighboring unit cells; $\lambda = 10.5$ Å; and $k = 1$ for $r_{ij} < 25$ Å and $k = 0$ otherwise (the nonzero value of k is arbitrary due to the normalization used below). Covariances of atom pair displacements $v_{ij} = \langle \mathbf{r}_i \cdot \mathbf{r}_j \rangle$ were obtained using the pseudoinverse of \mathbf{H} as described in ref. 64. The values of v_{ij} were renormalized to $\phi_{ij} = v_{ij} \sigma_i \sigma_j / (v_{ii} v_{jj})^{1/2}$ using the isotropic displacement parameters σ_i of the i th C_α atom from the Bragg refinement; the model was thus consistent with the refined crystal structure.

The diffuse intensity was computed as $D_{NM}(\mathbf{s}) = \sum_i \sum_j f_i f_j^* e^{-4\pi^2(\eta_i^2 + \eta_j^2) s^2} (e^{-4\pi^2 s^2 \psi_j} - 1)$, where f_i is the structure factor of the combined atoms in the residue associated with the i th C_α atom. Structure factors were computed using a two-Gaussian approximation of atomic form factors; the parameters were obtained using the `eltbx.X-ray_scattering` methods in CCTBX (62); phase factors were applied using the atomic coordinates.

The Bragg intensities were computed from ensembles generated by using the first 10 nonzero eigenvectors of **H** with corresponding inverse eigenvalues as their weights. Because the overall scale of the spring constant was arbitrary in the NM model (see above), the amplitudes of motion were too large using the absolute eigenvalues; they were therefore scaled to maintain the connectivity of the backbones. Fifty member ensemble models were generated by Normal Mode Wizard (NMWiz) (65), which is a VMD (66) plugin. A single B factor of 10 \AA^2 was applied to all atoms in the ensemble. Structure factors were generated using phenix.fmodel and compared with the experimental data using phenix.reflection_statistics (67).

ACKNOWLEDGMENTS. We thank Pavel Afonine for computational assistance in converting and comparing structure factors. We are grateful to the University of California, Office of the President, Multicampus Research Programs and Initiatives Grant MR-15-338599, and the Program for Breakthrough Biomedical Research, which is partially funded by the Sandler Foundation. Use of the Stanford Synchrotron Radiation Lightsource, SLAC National Accelerator Laboratory, is supported by the US Department of Energy, Office of Science, Office of Basic Energy Sciences, under Contract DE-AC02-76SF00515. The Stanford Synchrotron Radiation Lightsource Structural Molecular Biology Program is supported by the US Department of Energy.

Office of Biological and Environmental Research, and by the NIH, National Institute of General Medical Sciences (including P41GM103393). N.K.S. was supported by NIH Grant GM095887. J.S.F. was supported by a Searle Scholar Award from the Kinship Foundation, a Pew Scholar Award from the Pew Charitable Trusts, a Packard Fellowship from the David and Lucile Packard

Foundation, NIH Grant OD009180, NIH Grant GM110580, and National Science Foundation Grant STC-1231306. M.E.W. was supported by the US Department of Energy under Contract DE-AC52-06NA25396 through the Laboratory-Directed Research and Development Program at Los Alamos National Laboratory (LANL). The LANL technical release number is LA-UR-15-28934.

- van den Bedem H, Fraser JS (2015) Integrative, dynamic structural biology at atomic resolution—it's about time. *Nat Methods* 12(4):307–318.
- Clarage JB, Phillips GN, Jr (1997) Analysis of diffuse scattering and relation to molecular motion. *Methods Enzymol* 277:407–432.
- Keen DA, Goodwin AL (2015) The crystallography of correlated disorder. *Nature* 521(7552):303–309.
- Kuzmanic A, Kruschel D, van Gunsteren WF, Pannu NS, Zagrovic B (2011) Dynamics may significantly influence the estimation of interatomic distances in biomolecular X-ray structures. *J Mol Biol* 411(1):286–297.
- Schomaker V, Trueblood KN (1968) On the rigid-body motion of molecules in crystals. *Acta Crystallogr B* 24(1):63–76.
- Painter J, Merritt EA (2005) A molecular viewer for the analysis of TLS rigid-body motion in macromolecules. *Acta Crystallogr D Biol Crystallogr* 61(Pt 4):465–471.
- Painter J, Merritt EA (2006) Optimal description of a protein structure in terms of multiple groups undergoing TLS motion. *Acta Crystallogr D Biol Crystallogr* 62(Pt 4):439–450.
- Van Benschoten AH, et al. (2015) Predicting X-ray diffuse scattering from translation-libration-screw structural ensembles. *Acta Crystallogr D Biol Crystallogr* 71(Pt 8):1657–1667.
- Urzhumtsev A, Afonine PV, Van Benschoten AH, Fraser JS, Adams PD (2015) From deep TLS validation to ensembles of atomic models built from elemental motions. *Acta Crystallogr D Biol Crystallogr* 71(Pt 8):1668–1683.
- van den Bedem H, Bhabha G, Yang K, Wright PE, Fraser JS (2013) Automated identification of functional dynamic contact networks from X-ray crystallography. *Nat Methods* 10(9):896–902.
- Burnley BT, Afonine PV, Adams PD, Gros P (2012) Modelling dynamics in protein crystal structures by ensemble refinement. *eLife* 1:e00311.
- Ma P, et al. (2015) Observing the overall rocking motion of a protein in a crystal. *Nat Commun* 6:8361.
- Wall ME, et al. (2014) Conformational dynamics of a crystalline protein from microsecond-scale molecular dynamics simulations and diffuse X-ray scattering. *Proc Natl Acad Sci USA* 111(50):17887–17892.
- Janowski PA, Liu C, Deckman J, Case DA (2016) Molecular dynamics simulation of tricinlic lysozyme in a crystal lattice. *Protein Sci* 25(1):87–102.
- Janowski PA, Cerutti DS, Holton J, Case DA (2013) Peptide crystal simulations reveal hidden dynamics. *J Am Chem Soc* 135(21):7938–7948.
- James R (1948) *The Optical Principles of the Diffraction of X-rays* (Bell, London).
- Guinier A (1963) *X-ray Diffraction in Crystals, Imperfect Crystals, and Amorphous Bodies* (W.H. Freeman and Co., San Francisco).
- Wall ME, Clarage JB, Phillips GN (1997) Motions of calmodulin characterized using both Bragg and diffuse X-ray scattering. *Structure* 5(12):1599–1612.
- Caspar DL, Clarage J, Salunke DM, Clarage M (1988) Liquid-like movements in crystalline insulin. *Nature* 332(6165):659–662.
- Clarage JB, Clarage MS, Phillips WC, Sweet RM, Caspar DL (1992) Correlations of atomic movements in lysozyme crystals. *Proteins* 12(2):145–157.
- Wall ME, Ealick SE, Gruner SM (1997) Three-dimensional diffuse X-ray scattering from crystals of staphylococcal nuclease. *Proc Natl Acad Sci USA* 94(12):6180–6184.
- Moore PB (2009) On the relationship between diffraction patterns and motions in macromolecular crystals. *Structure* 17(10):1307–1315.
- Doucet J, Benoit JP (1987) Molecular dynamics studied by analysis of the X-ray diffuse scattering from lysozyme crystals. *Nature* 325(6105):643–646.
- Pérez J, Faure P, Benoit JP (1996) Molecular rigid-body displacements in a tetragonal lysozyme crystal confirmed by X-ray diffuse scattering. *Acta Crystallogr D Biol Crystallogr* 52(Pt 4):722–729.
- Yang L, Song G, Jernigan RL (2007) How well can we understand large-scale protein motions using normal modes of elastic network models? *Biophys J* 93(3):920–929.
- Kidera A, Matsushima M, Gö N (1994) Dynamic structure of human lysozyme derived from X-ray crystallography: Normal mode refinement. *Biophys Chem* 50(1-2):25–31.
- Ni F, Poon BK, Wang Q, Ma J (2009) Application of normal-mode refinement to X-ray crystal structures at the lower resolution limit. *Acta Crystallogr D Biol Crystallogr* 65(Pt 7):633–643.
- Lu M, Ma J (2008) A minimalist network model for coarse-grained normal mode analysis and its application to biomolecular X-ray crystallography. *Proc Natl Acad Sci USA* 105(40):15358–15363.
- Gniewek P, Kolinski A, Jernigan RL, Kloczkowski A (2012) Elastic network normal modes provide a basis for protein structure refinement. *J Chem Phys* 136(19):195101.
- Poon BK, et al. (2007) Normal mode refinement of anisotropic thermal parameters for a supramolecular complex at 3.42-Å crystallographic resolution. *Proc Natl Acad Sci USA* 104(19):7869–7874.
- Faure P, et al. (1994) Correlated intramolecular motions and diffuse X-ray scattering in lysozyme. *Nat Struct Biol* 1(2):124–128.
- Mizuguchi K, Kidera A, Gö N (1994) Collective motions in proteins investigated by X-ray diffuse scattering. *Proteins* 18(1):34–48.
- Riccardi D, Cui Q, Phillips GN, Jr (2010) Evaluating elastic network models of crystalline biological molecules with temperature factors, correlated motions, and diffuse X-ray scattering. *Biophys J* 99(8):2616–2625.
- Meinhold L, Smith JC (2007) Protein dynamics from X-ray crystallography: Anisotropic, global motion in diffuse scattering patterns. *Proteins* 66(4):941–953.
- Meinhold L, Smith JC (2005) Correlated dynamics determining X-ray diffuse scattering from a crystalline protein revealed by molecular dynamics simulation. *Phys Rev Lett* 95(21):218103.
- Meinhold L, Smith JC (2005) Fluctuations and correlations in crystalline protein dynamics: A simulation analysis of staphylococcal nuclease. *Biophys J* 88(4):2554–2563.
- Meinhold L, Merzel F, Smith JC (2007) Lattice dynamics of a protein crystal. *Phys Rev Lett* 99(13):138101.
- Clarage JB, Romo T, Andrews BK, Pettitt BM, Phillips GN, Jr (1995) A sampling problem in molecular dynamics simulations of macromolecules. *Proc Natl Acad Sci USA* 92(8):3288–3292.
- Héry S, Genest D, Smith JC (1998) X-ray diffuse scattering and rigid-body motion in crystalline lysozyme probed by molecular dynamics simulation. *J Mol Biol* 279(1):303–319.
- Welberry TR (2004) *Diffuse X-ray Scattering and Models of Disorder* (Oxford Univ Press, Oxford).
- Phillips GN, Jr, Fillers JP, Cohen C (1980) Motions of tropomyosin. Crystal as metaphor. *Biophys J* 32(1):485–502.
- Chacko S, Phillips GN, Jr (1992) Diffuse X-ray scattering from tropomyosin crystals. *Biophys J* 61(5):1256–1266.
- Helliwell J, Glover I, Jones A, Pantos E, Moss D (1986) Protein dynamics: Use of computer graphics and protein crystal diffuse scattering recorded with synchrotron X-radiation. *Biochem Soc Trans* 14(3):653–655.
- Kolatkhar AR, Clarage JB, Phillips GN, Jr (1994) Analysis of diffuse scattering from yeast initiator tRNA crystals. *Acta Crystallogr D Biol Crystallogr* 50(Pt 2):210–218.
- Welberry TR, Heerdegen AP, Goldstone DC, Taylor IA (2011) Diffuse scattering resulting from macromolecular frustration. *Acta Crystallogr B* 67(Pt 6):516–524.
- Polikanov YS, Moore PB (2015) Acoustic vibrations contribute to the diffuse scatter produced by ribosome crystals. *Acta Crystallogr D Biol Crystallogr* 71(Pt 10):2021–2031.
- Gruner SM (2012) X-ray imaging detectors. *Phys Today* 65(12):29–34.
- Wall ME, Adams PD, Fraser JS, Sauter NK (2014) Diffuse X-ray scattering to model protein motions. *Structure* 22(2):182–184.
- Fraser JS, et al. (2011) Accessing protein conformational ensembles using room-temperature X-ray crystallography. *Proc Natl Acad Sci USA* 108(39):16247–16252.
- Chaudhry C, Horwich AL, Brunger AT, Adams PD (2004) Exploring the structural dynamics of the *E. coli* chaperonin GroEL using translation-libration-screw crystallographic refinement of intermediate states. *J Mol Biol* 342(1):229–245.
- Henzler-Wildman KA, et al. (2007) Intrinsic motions along an enzymatic reaction trajectory. *Nature* 450(7171):838–844.
- Bahar I, Lezon TR, Yang LW, Eyal E (2010) Global dynamics of proteins: Bridging between structure and function. *Annu Rev Biophys* 39:23–42.
- Keedy DA, Fraser JS, van den Bedem H (2015) Exposing hidden alternative backbone conformations in X-ray crystallography using qFit. *PLoS Comput Biol* 11(10):e1004507.
- van den Bedem H, Dhanik A, Latombe JC, Deacon AM (2009) Modeling discrete heterogeneity in X-ray diffraction data by fitting multi-conformers. *Acta Crystallogr D Biol Crystallogr* 65(Pt 10):1107–1117.
- Burling FT, Brünger AT (1994) Thermal motions and conformational disorder in protein crystal structures: Comparison of multi-conformer and time-averaging models. *Israeli J Chem* 34:165–175.
- Kuriyan J, et al. (1991) Exploration of disorder in protein structures by X-ray restrained molecular dynamics. *Proteins* 10(4):340–358.
- Clarage JB, Phillips GN, Jr (1994) Cross-validation tests of time-averaged molecular dynamics refinements for determination of protein structures by X-ray crystallography. *Acta Crystallogr D Biol Crystallogr* 50(Pt 1):24–36.
- Wilson MA (2013) Visualizing networks of mobility in proteins. *Nat Methods* 10(9):835–837.
- Gaffney KJ, Chapman HN (2007) Imaging atomic structure and dynamics with ultrafast x-ray scattering. *Science* 316(5830):1444–1448.
- Wall ME (2009) Methods and software for diffuse X-ray scattering from protein crystals. *Methods Mol Biol* 544:269–279.
- Parkhurst JM, et al. (2014) dxtbx: The diffraction experiment toolbox. *J Appl Cryst* 47(Pt 4):1459–1465.
- Grosse-Kunstleve RW, Sauter NK, Moriarty NW, Adams PD (2002) The Computational Crystallography Toolbox: Crystallographic algorithms in a reusable software framework. *J Appl Cryst* 35(1):126–136.
- Arvai A (2012) ADXV—a program to display X-ray diffraction images (Scripps Research Institute, La Jolla, CA).
- Atilgan AR, et al. (2001) Anisotropy of fluctuation dynamics of proteins with an elastic network model. *Biophys J* 80(1):505–515.
- Bakan A, Meireles LM, Bahar I (2011) ProDy: Protein dynamics inferred from theory and experiments. *Bioinformatics* 27(11):1575–1577.
- Humphrey W, Dalke A, Schulten K (1996) VMD: Visual molecular dynamics. *J Mol Graph* 14(1):33–38, 27–28.
- Adams PD, et al. (2010) PHENIX: A comprehensive Python-based system for macromolecular structure solution. *Acta Crystallogr D Biol Crystallogr* 66(Pt 2):213–221.

Table S1 – Comparison of CypA observed Bragg data vs. calculated from Normal Modes.

Resolution (Å)	R-factor	CC
44.560-11.070	0.5713	0.4144
11.070-8.698	0.3325	0.6957
8.697-6.834	0.2987	0.7324
6.831-5.369	0.2944	0.788
5.366-4.217	0.2556	0.8362
4.216-3.314	0.2592	0.8153
3.312-2.603	0.3092	0.7586
2.602-2.045	0.3355	0.6972
2.045-1.606	0.3602	0.6928
1.606-1.262	0.41	0.5964
1.262-1.200	0.4509	0.3817
All	0.3869	0.855

Table S2 - Comparison of Trypsin observed Bragg data vs. calculated from Normal Modes.

Resolution (Å)	R-factor	CC
26.837-10.849	0.511	0.4285
10.837-8.689	0.3368	0.7372
8.678-6.955	0.3786	0.6475
6.937-5.569	0.3312	0.7195
5.564-4.457	0.2509	0.8368
4.455-3.569	0.2322	0.8663
3.568-2.857	0.2684	0.8155
2.857-2.288	0.2924	0.761
2.288-1.832	0.2911	0.7678
1.832-1.467	0.3072	0.7564
1.467-1.200	0.3271	0.7048
All	0.3106	0.887

Table S3. Refinement statistics for CypA and trypsin models, before TLS modeling is applied.

	CypA	Trypsin
Resolution range, Å	38.66-1.4	23.29-1.25
Space group	P 21 21 21	P 21 21 21
Unit cell, Å	42.91, 52.44, 89.12	54.81, 58.51, 67.42
Completeness (%)	98	95
R _{work} (%)	17.88	15.9
R _{free} (%)	19.5	17.41
RMS (bonds, Å)	0.007	0.013
RMS (angles, degrees)	1.16	1.61
Ramachandran favored %	97	98
Ramachandran allowed %	3	2
Ramachandran outliers %	0	0
Clashscore	0.79	2.59
Average B-factor, Å ²	21.42	14.57

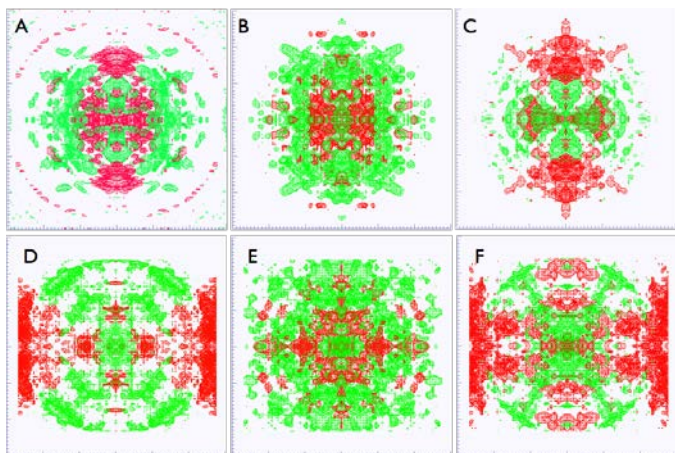


Figure S1. Visualization of anisotropic diffuse intensities. (A) Symmetrized CypA experimental data with isosurfaces shown using wireframes at a level of 2 photon counts in the resolution range 4.16 Å – 2.97 Å. Positive intensity is rendered in green, negative in red. (B) Isosurfaces for diffuse scattering predicted by the CypA LLM model. (C) Residual diffuse scattering (experimental data (A) minus LLM (B)). (D) Symmetrized Trypsin experimental data with isosurfaces shown using wireframes at a level of 3 photon counts in the resolution range 4.53 Å – 3.26. (E) Isosurfaces for diffuse scattering predicted by the Trypsin LLM model. (F) Residual diffuse scattering (experimental data (D) minus LLM (E)).

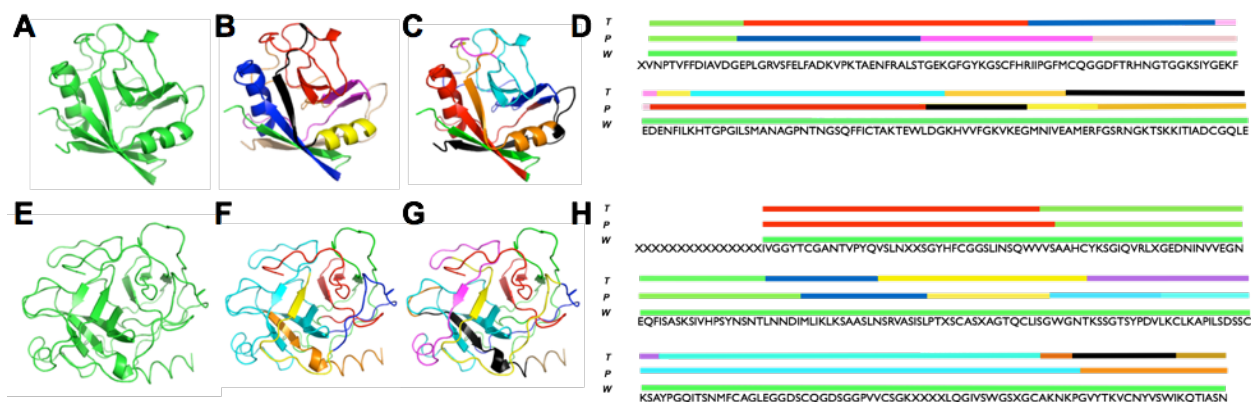


Figure S2. Rigid body domain definitions used for TLS models. CypA and Trypsin TLS groups shown on the tertiary structure for whole molecule (A, E), Phenix (B, F), and TLSMD (C, G) and shown on the primary sequence (D, H).

Figure S3: Simulated diffraction images for trypsin frame 45 obtained using: (A) liquid-like motions model; (B) integrated 3D diffuse data; (C) elastic network model.

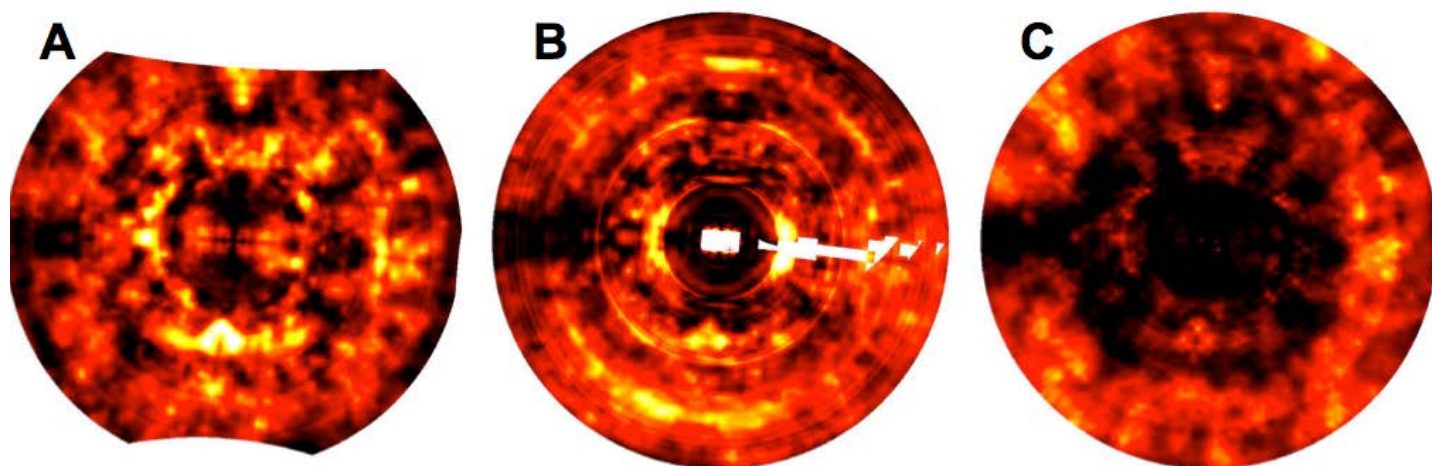


Figure S4: Normal modes models for a) CypA and b) Trypsin. The RCSB deposited structure is shown in blue with thicker ribbon. Every 5th ensemble member of the 50 member ensemble is shown in a different color. Displacements along the top 10 modes are shown with the sum of squares of displacements equal to 1 Å.

A



B

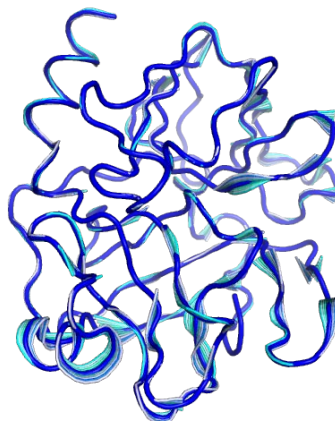


Figure S5: Simulation of CypA diffraction images using integrated 3D data. Left: raw processed frame 67, after the mode filter step (Methods). Middle: isosurface in anisotropic diffuse intensity at a level of 2 photons, displayed using ParaView (<http://www.paraview.org/>). Right: Simulated diffuse intensity for frame 67 computed using 3D diffuse intensity. For each image, the minimum value within each pixel-width ring about origin has been subtracted from each pixel value, to enhance the visualization of anisotropic diffuse features. Images are displayed using a heat map in Adxv.

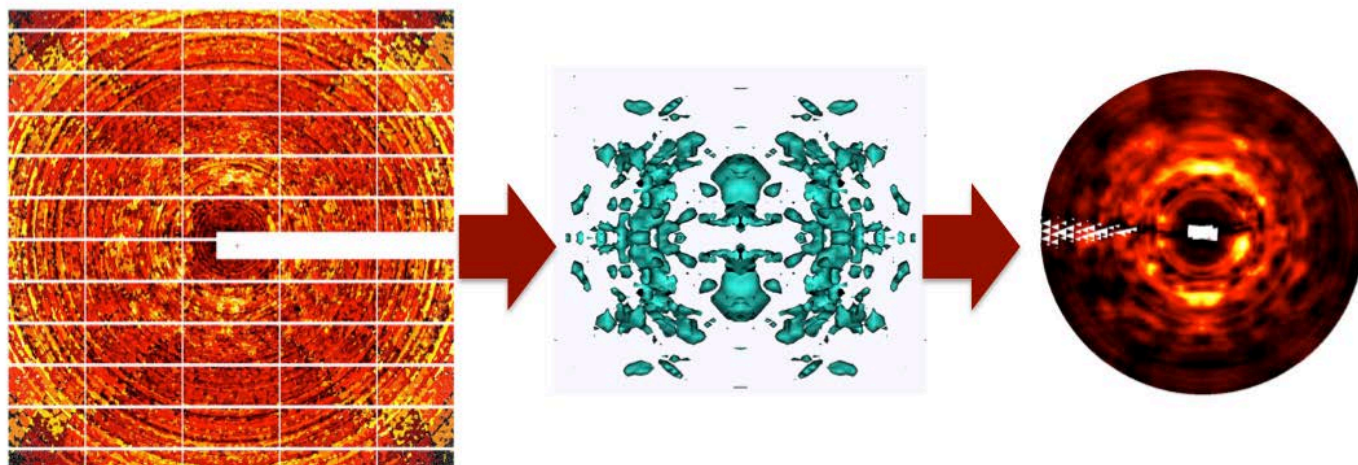
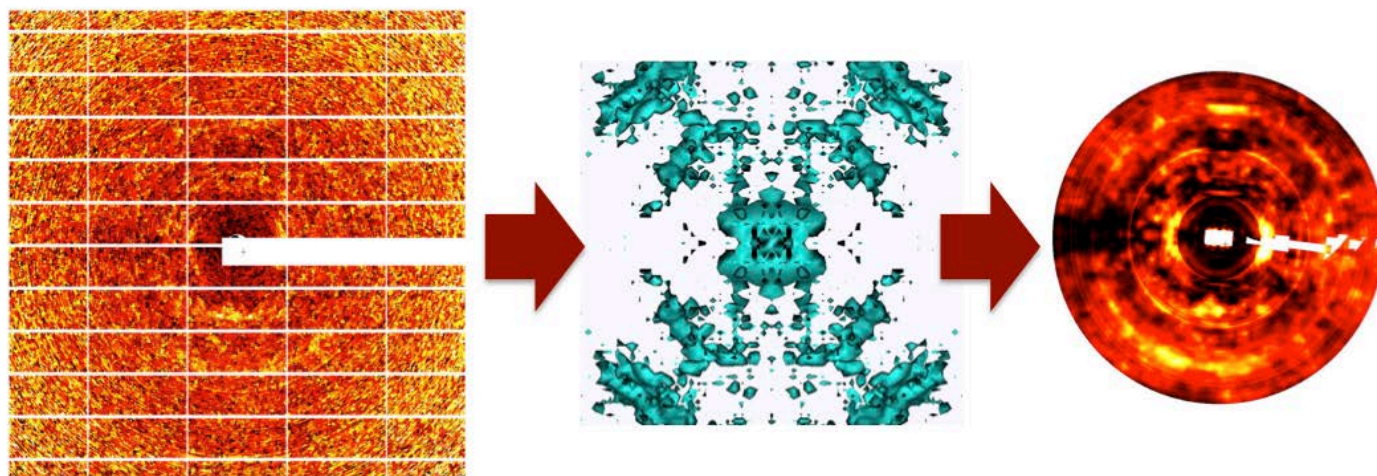


Figure S6: Simulation of trypsin diffraction images using integrated 3D data. Left: raw processed frame 45, after the mode filter step (Methods). Middle: isosurface in anisotropic diffuse intensity at a level of 3 photons, displayed using ParaView (<http://www.paraview.org/>). Right: Simulated diffuse intensity for frame 45 computed using 3D diffuse intensity. Images were processed and displayed as in Fig. S6.



Supplementary Text

Methods

Protein purification and crystallization

Trypsin crystals were obtained according to the method of Liebschner *et.al* (1). Lyophilized bovine pancreas trypsin was purchased from Sigma-Aldrich (T1005) and dissolved at a concentration of 30 mg/mL into 30mM HEPES pH 7.0, 5 mg/mL benzamidine and 3mM CaCl₂. Crystals were obtained from a solution of 200mM Ammonium sulfate, 100mM Na cacodylate pH 6.5, 20% PEG 8000 and 15% glycerol. CypA was purified and crystallized as previously described (2). Briefly, the protein was concentrated to 60 mg/mL in 20mM HEPES pH 7.5, 100mM NaCl and 500mM TCEP. Trays were set with a precipitant solution of 100mM HEPES pH 7.5, 22% PEG 3350 and 5mM TCEP. Both crystal forms were obtained using the hanging-drop method.

Crystallographic data collection

Diffraction data were collected on beamline 11-1 at the Stanford Synchrotron Radiation Lightsource (Menlo Park, CA). X-ray diffraction images were obtained using a Dectris PILATUS 6M Pixel Array Detector (PAD). Each dataset was collected from a single crystal at an ambient temperature of 273K. To prevent dehydration, crystals were coated in a thin film of paratone with minimal surrounding mother liquor. For CypA, a single set of 0.5 degree oscillation images were collected and used for both Bragg and diffuse data processing. A total of 360 images were collected across a 180 degree phi rotation. The Trypsin diffraction data consisted of one degree oscillations across a 135 degree phi rotation; this dataset was similarly used for both Bragg and diffuse data analysis. Both datasets were collected to optimize the Bragg signal, not the diffuse signal. Although not used here, we note that data collection using a PAD with fine phi slicing should be especially well suited for simultaneous collection of Bragg and diffuse data, as it would enable integration of diffuse intensity at a tunable level of detail in reciprocal space.

Bragg data processing

Bragg diffraction data were processed using XDS and XSCALE (3) within the *xia2* software package (4). Molecular replacement solutions were found using Phaser (5) within the *Phenix* software suite (6). The PDB search models were 4I8G for trypsin, and 2CPL for CypA. Initial structural refinement was performed using *phenix.refine* (7). The strategy included refinement of individual atomic coordinates and water picking. Both the X-ray/atomic displacement parameters and X-ray/stereochemistry weights were optimized. Isotropic B-factors were chosen for the initial structures to allow for non-negligible R-factor optimization by subsequent TLS refinement strategies. All structures were refined for a total of 5 macrocycles. Statistics for these initial crystal structure models are shown in Supplementary **Table S3** and are available along with the structures at www.rcsb.org in PDB entries 5F66 (CypA) and 5F6M (trypsin).

Supplementary References:

1. Liebschner D, Dauter M, Brzuszkiewicz A, & Dauter Z (2013) On the reproducibility of protein crystal structures: five atomic resolution structures of trypsin. *Acta Crystallogr D Biol Crystallogr* 69(Pt 8):1447-1462.
2. Fraser JS, *et al.* (2009) Hidden alternative structures of proline isomerase essential for catalysis. *Nature* 462(7273):669-673.
3. Kabsch W (2010) Xds. *Acta Crystallogr D Biol Crystallogr* 66(Pt 2):125-132.
4. Winter G, Lobley CM, & Prince SM (2013) Decision making in xia2. *Acta Crystallogr D Biol Crystallogr* 69(Pt 7):1260-1273.

5. McCoy AJ, *et al.* (2007) Phaser crystallographic software. *J Appl Crystallogr* 40(Pt 4):658-674.
6. Adams PD, *et al.* (2010) PHENIX: a comprehensive Python-based system for macromolecular structure solution. *Acta Crystallogr D Biol Crystallogr* 66(Pt 2):213-221.
7. Afonine PV, *et al.* (2012) Towards automated crystallographic structure refinement with phenix.refine. *Acta Crystallogr D Biol Crystallogr* 68(Pt 4):352-367.